

# Zenithal bistable liquid-crystal gratings as tunable beam splitters

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# Overview

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  - Zenithal Bistable Devices
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- 3 Liquid Crystal Zenithal Bistable Gratings
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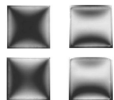
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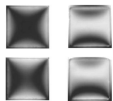


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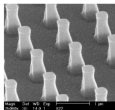
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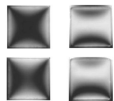


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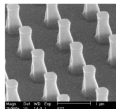
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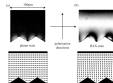
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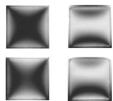
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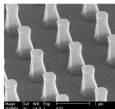
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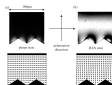
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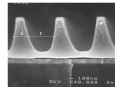
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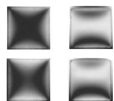


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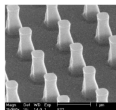
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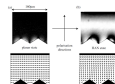
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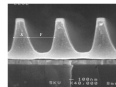
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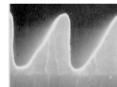
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[Handbook of Visual Display Technology,  
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## The ZBD<sup>©</sup> display



- Zero idle consumption, high tolerance to mechanical stress, no image sticking, fabrication in TN-LCD production lines...

[Handbook of Visual Display Technology, 1507-1543, Springer, 2012]

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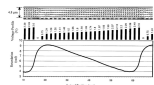
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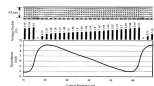


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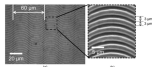
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## Electro-optic control



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## Periodic alignment pattern

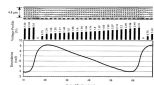


[Opt. Express 3, 3034  
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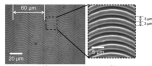
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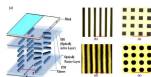
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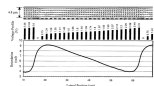


[Opt. Lett. 38, 2342  
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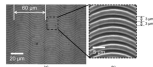
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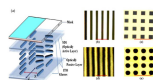
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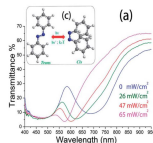
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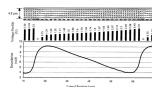


[J. Mater. Chem C 2,  
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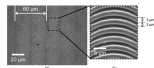
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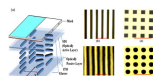
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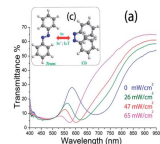
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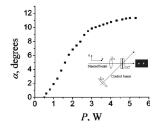
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[J. Mater. Chem C 2,  
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## All-optical non-linear switching



[Appl. Phys. Lett. 84,  
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- **Zero idle power, very low switching power consumption, no need for complicated alignment patterns, masks, high power pump/control optical beams. Ease of integration.**
- Can leverage on the mature **LCD/ZBD fabrication technology.**
- Need for rigorous numerical tools: **a) LC orientation in bistable devices, b) optical/diffraction studies, c) Optimization procedure to achieve target results.**

# The Q-tensor model for LC studies

- The orientation of the nematic molecules is expressed via the  $3 \times 3$  symmetric tensor  $\mathbf{Q}$ , which is the traceless part of the second moment of the probability density function matrix.

$$\mathbf{Q} = \begin{pmatrix} q_1 & q_2 & q_3 \\ q_2 & q_4 & q_5 \\ q_3 & q_5 & -q_1 - q_4 \end{pmatrix}$$

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- In the general case of biaxial solutions, it can be decomposed into two directors and two order parameters,

$$\mathbf{Q} = S_1 (\mathbf{n} \otimes \mathbf{n}) + S_2 (\mathbf{m} \otimes \mathbf{m}) - \frac{1}{3} (S_1 + S_2) \mathbf{I}$$

# The Q-tensor model for LC studies

- The free energy in the LC bulk is expressed as

$$F = \iiint_V F_b dV = \iiint_V (F_{\text{th}} + F_{\text{el}} + F_{\text{em}}) dV$$

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- The free energy is minimized via the solution of the Euler-Lagrange equations

$$\sum_{j=1}^3 \frac{\partial}{\partial x_j} \left( \frac{\partial F_b}{\partial q_{i,j}} \right) - \frac{\partial F_b}{\partial q_i} = \gamma_1^* \frac{\partial D}{\partial \dot{q}_i},$$

for  $i = 1...5$ , where  $q_{i,j} = \partial q_i / \partial x_j$ ,  $x_j$  being the unit vectors of the three-dimensional cartesian system. The r.h.s. of (9) describes the dynamic evolution of the  $\mathbf{Q}$  tensor via the dissipation function  $D = \text{tr}(\dot{\mathbf{Q}}^2)$ , where  $\dot{\mathbf{Q}} = \partial \mathbf{Q} / \partial t$ . The term  $\gamma_1^*$  is related to the LC rotational viscosity  $\gamma_1$  via  $\gamma_1^* = \gamma_1 / (4S_{\text{exp}}^2)$

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- The thermotropic energy  $F_{\text{th}}$  is expressed via a Taylor expansion around  $\mathbf{Q}$

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- The elastic energy is described by

$$F_{\text{el}} = \sum_{i,j,k=1,2,3} \left[ \frac{L_1}{2} \left( \frac{\partial Q_{ij}}{\partial x_k} \right)^2 + \frac{L_2}{2} \frac{\partial Q_{ij}}{\partial x_j} \frac{\partial Q_{ik}}{\partial x_k} \right] + \sum_{i,j,k,l=1,2,3} \left[ \frac{L_6}{2} Q_{lk} \frac{\partial Q_{ij}}{\partial x_l} \frac{\partial Q_{ij}}{\partial x_k} \right]$$

The elastic parameters  $L_i$  are related to the Frank elastic constants  $K_{ij}$  via the expressions  $L_1 = (K_{33} - K_{11} + 3K_{22}) / (6S_{\text{exp}}^2)$ ,  $L_2 = (K_{11} - K_{22}) / S_{\text{exp}}^2$ , and  $L_6 = (K_{33} - K_{11}) / (2S_{\text{exp}}^3)$ .



# The Q-tensor model for LC studies

- The electrostatic energy in the presence of an external electric field is given by

$$F_{\text{em}} = - \int \mathbf{D} \cdot d\mathbf{E},$$

The displacement field is given by the constitutive equation

$$\mathbf{D} = \varepsilon_0 \tilde{\varepsilon}_r \mathbf{E} + \mathbf{P}_s,$$

For nematic materials the dielectric tensor is given by

$$\tilde{\varepsilon}_r = \Delta\varepsilon^* \mathbf{Q} + \bar{\varepsilon} \mathbf{I},$$

where  $\Delta\varepsilon^* = (\varepsilon_{\parallel} - \varepsilon_{\perp})/S_{\text{exp}}$  is the scaled dielectric anisotropy and  $\bar{\varepsilon} = (\varepsilon_{\parallel} + 2\varepsilon_{\perp})/3$ .

# The Q-tensor model for LC studies

- The spontaneous polarization  $\mathbf{P}_s$  derives from the flexoelectric effect:

$$P_i = p_1 \sum_{j=1,2,3} \frac{\partial Q_{ij}}{\partial x_j} + p_2 \sum_{j,k=1,2,3} Q_{ij} \frac{\partial Q_{jk}}{\partial x_k},$$

where  $p_1 = (e_{11} + e_{33})/(2S_{\text{exp}})$  and  $p_2 = (e_{11} - e_{33})/(2S_{\text{exp}}^2)$  are terms depending on the classical flexoelectric polarization coefficients  $e_{11}$  and  $e_{33}$ , as in

$$\mathbf{P}_s = e_{11} (\nabla \cdot \mathbf{n}) \mathbf{n} + e_{33} (\nabla \times \mathbf{n}) \times \mathbf{n},$$

where  $\mathbf{n}$  is the nematic director.

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In this work, the nematic material of choice is E7, characterized by:

- Thermotropic coefficients:  $a = -0.3 \times 10^5 \text{ J/m}^3$ ,  
 $b = -1.5 \times 10^5 \text{ J/m}^3$ , and  $c = 2.5 \times 10^5 \text{ J/m}^3$
- Elastic coefficients:  $K_{11} = 10.3 \text{ pN}$ ,  $K_{22} = 7.4 \text{ pN}$ , and  
 $K_{33} = 16.48 \text{ pN}$
- Dielectric properties:  $\varepsilon_{\parallel} = 18.6$ ,  $\varepsilon_{\perp} = 5.31$ ,  
 $e_{11} + e_{33} = 15 \text{ pC/m}$ , and  $e_{11} - e_{33} = 10 \text{ pC/m}$
- Rotational viscosity:  $\gamma_1 = 282.8 \text{ mPa}$

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- 3 The  $x$ -component of  $\mathbf{E}^t$  is expanded in a 1-D Floquet series according to

$$E_x^t(x, y = y_0) = \sum_m E_{x,m}^t e^{-j\beta_m y},$$

where  $\beta_m = \beta_0 + 2\pi m/p_0$ ,  $\beta_0 = (2\pi n_g/\lambda_0) \sin(\theta_{\text{inc}})$  being the polymer wavenumber projection in the direction of periodicity ( $x$ -axis) for the general case of oblique incidence at an angle  $\theta_{\text{inc}}$ .



# Diffraction efficiency calculation in optical gratings

- ④ The amplitudes  $E_{x,m}^t$  are obtained from orthogonality considerations with an integration over a grating period

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- 5 Finally, the total diffraction efficiency for each diffraction mode is calculated by

$$DE_m = \frac{P_m}{P^i} = \frac{|E_{x,m}^t|^2}{|E_x^i|^2 |\cos \theta_m|},$$

where  $P^i$ ,  $E_x^i$  are the power and amplitude of the incident electric field, respectively, and  $\cos \theta_m$  is given by

$$\cos \theta_m = \frac{\sqrt{(k_0 n_g)^2 - \beta_m^2}}{k_0 n_g},$$

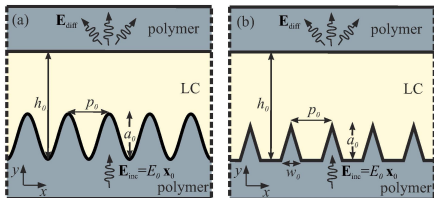
where  $k_0 = 2\pi/\lambda$  is the free space wavenumber.

# Liquid Crystal Zenithal Bistable Beam Splitters

- Structural layout: sinusoidal and triangular gratings

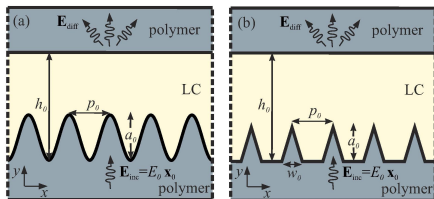
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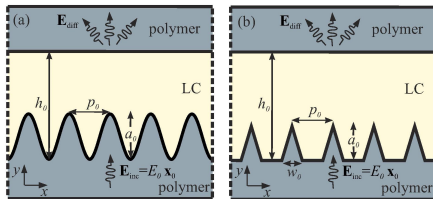
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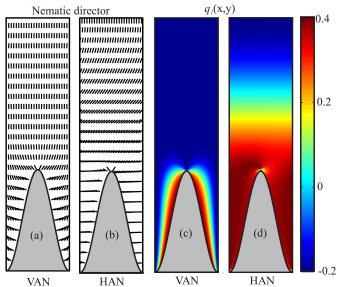
- **Objective:** minimize diffraction in one of the LC stable states and achieve **equal power splitting (two to five beams)** in the complimentary state.

# Liquid Crystal Zenithal Bistable Beam Splitters

- The sinusoidal ZB-LC grating shows two stable states with low (HAN) and high (VAN) tilt angle values.

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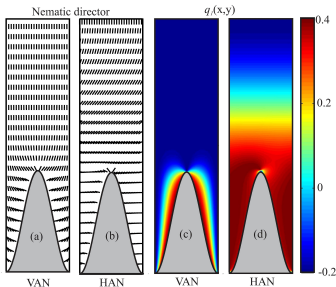
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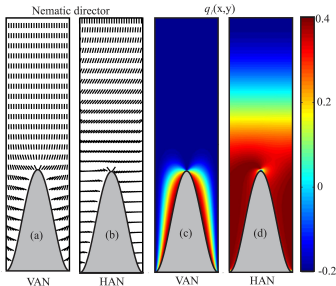
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- Defects are formed at the peak and trough of the grating for the HAN state.
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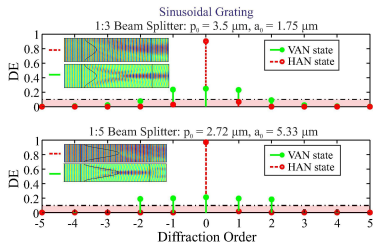
- **Matching condition:** we opt for a polymer material whose refractive index  $n_p$  is equal to the LC extraordinary index  $n_e = 1.73$  for E7 at 633 nm. This minimizes diffraction in the HAN state.

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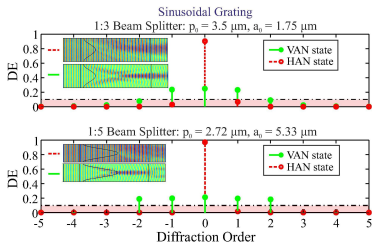
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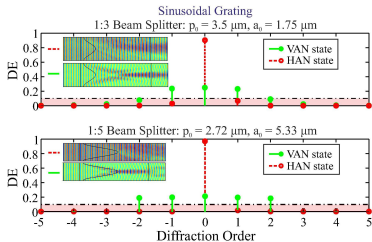
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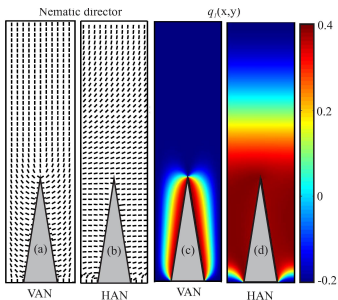
- Efficient beam splitting in **three** and **five** beams is demonstrated for the optimized grating designs.

# Liquid Crystal Zenithal Bistable Beam Splitters

- Triangular gratings offer an extra degree of freedom in the design: the basis of the triangular elements.

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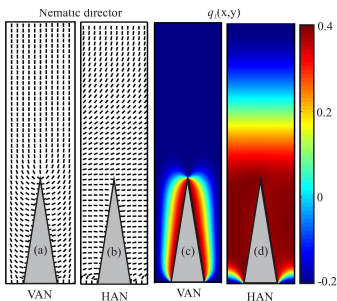
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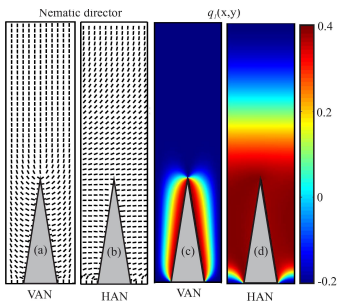
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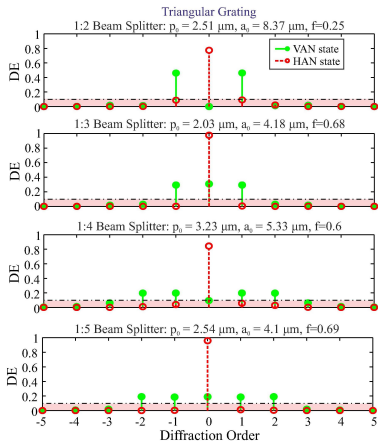
- The same optimization method is implemented: the parameter space is composed by the grating pitch  $p_0$ , the height  $a_0$  and the filling factor  $f = w_0/p_0$ .

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- The triangular grating offers a wider range of functionalities: **two to five beam splitting** is achieved.

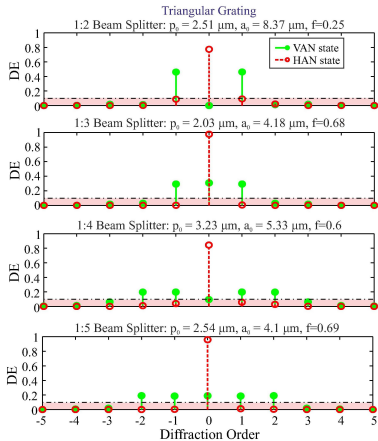
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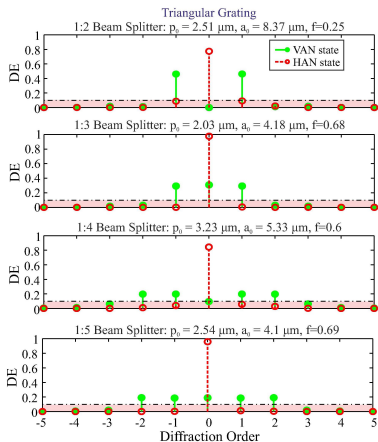
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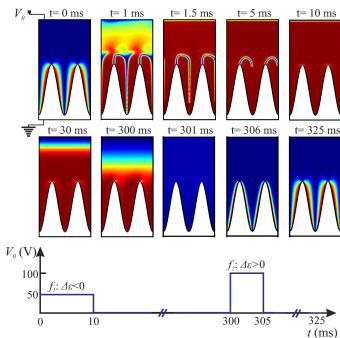
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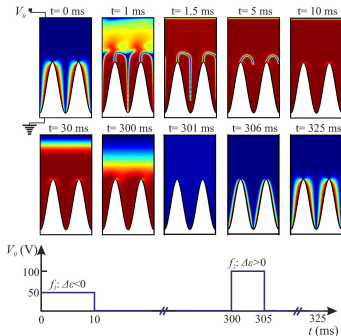
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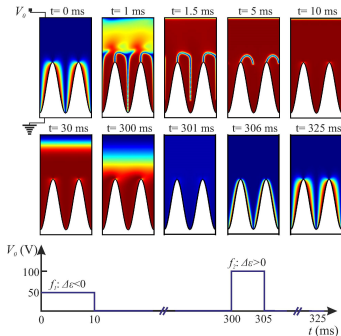
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- Control voltage is applied across the the 1  $\rightarrow$  3 sinusoidal grating via two ITO films.
- The grating is initially in the VAN state.
- A 10–ms 50 V pulse is applied at a frequency  $f_1 : \Delta\epsilon < 0$  at  $t = 0$ , followed by a 5–ms 100 V pulse at  $f_1 : \Delta\epsilon > 0$  at  $t = 300$  ms.

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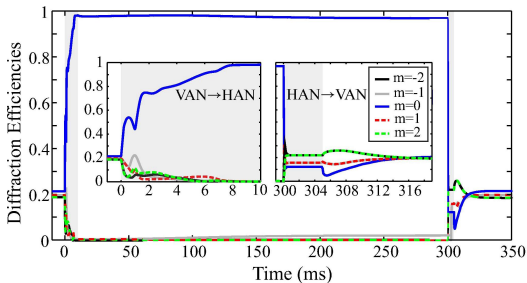
- Among the two transitions, **the VAN to HAN is much slower (100s of ms)**.

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- What is the impact of the LC dynamics on the grating's diffractive properties?

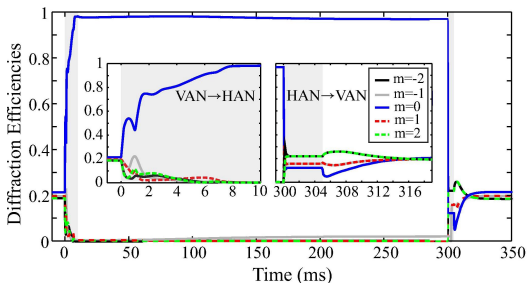
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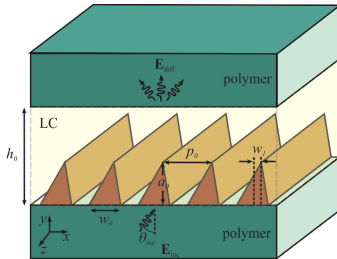
- The intermediate states during the VAN to HAN transition are **non-diffracting**.
- The overall **switching speed** of the device is governed by the HAN to VAN dynamics, **in the range of 10 ms**.

# Liquid Crystal Zenithal Bistable Beam Steerers

- Structural layout: blazed triangular grating

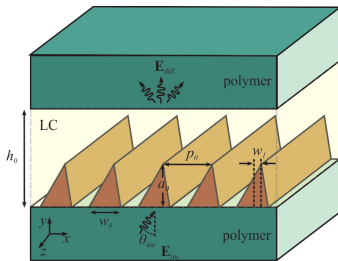
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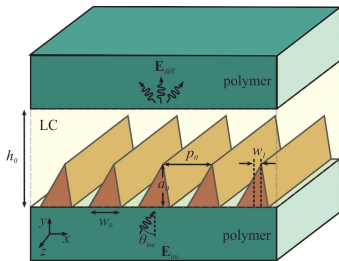


- Grating parameters: pitch  $p_0$ , height  $a_0$ , base  $w_0$ , blazing offset  $w_1$ .
- The nematic LC is E7. The polymer index  $n_p$  is matched to the LC extraordinary index  $n_e$ .
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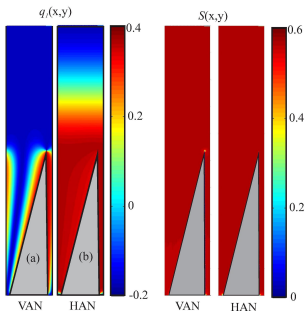
- **Objective:** minimize diffraction in the HAN state and maximize it in the VAN state along a **single diffraction order**.

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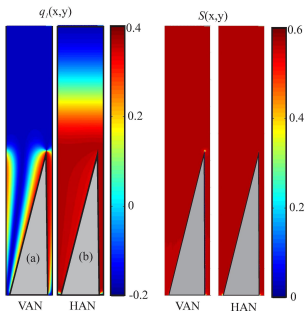
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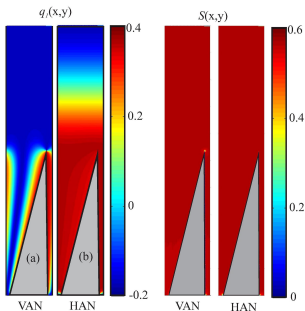
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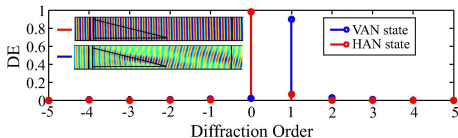
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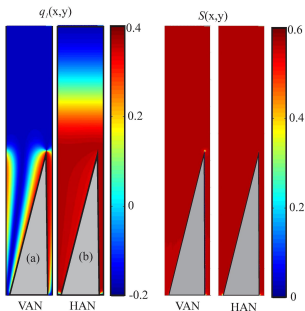


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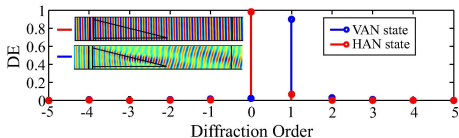


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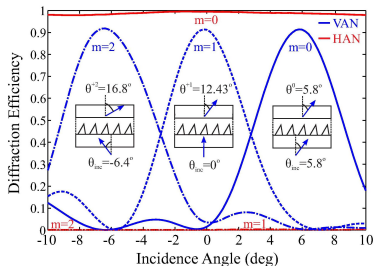
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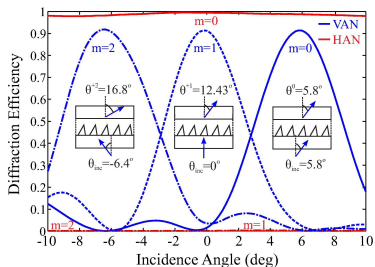
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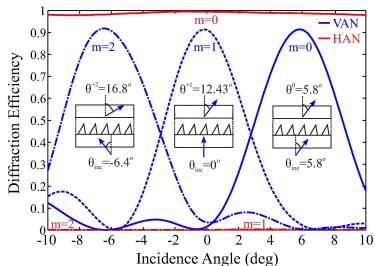
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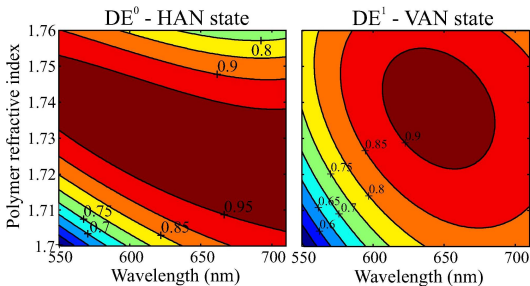
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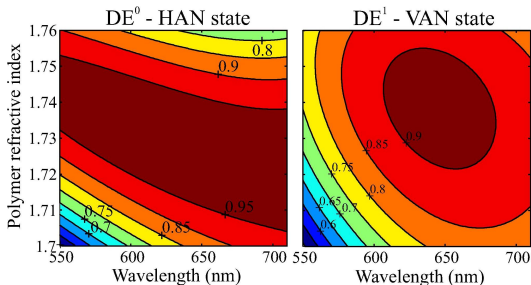
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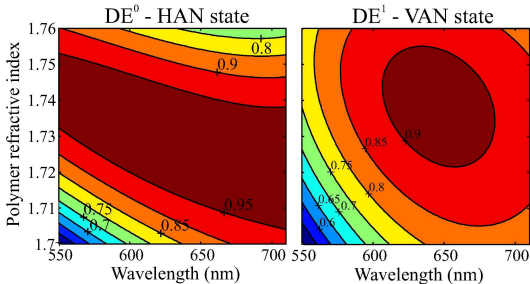
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- The non-resonant nature of the diffraction mechanism leads to increased robustness/broad bandwidths.

# Conclusions

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# Acknowledgments

## Financial Support

This work was supported by the **Italian Ministry of Foreign Affairs, Directorate General for the Country Promotion** and by the **European Union (European Social Fund-ESF) and Greek national funds** through the Operational Program Education and Lifelong Learning of the National Strategic Reference Framework (NSRF) Research Funding Program THALES Reinforcement of the interdisciplinary and/or inter-institutional research and innovation (Project ANEMOS).



*Ministero degli Affari Esteri*

